

# Estimation of age-standardized survival, even when age-specific data are sparse

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# Motivation

Age-  
standardized  
survival

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- Relative (net) survival approaches are typically used for population-based cancer data to ensure fair comparison.
- Common practice to age-standardise survival estimates in order to allow direct comparability across regions, countries, time-periods or other population groups.
- Sparsity creates difficulties for the standard approaches of age-standardisation.
- Trying to estimate net measures from real-world data - depletion due to other causes.

# Traditional age-standardization approaches

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- Weighted average of separate survival estimates for each age-group.
- Requires net survival estimates for all time-points for all age-groups.
- Estimating excess mortality can be hampered by high competing mortality, or low numbers initially.
- Typically now done using a Pohar Perme estimate in each age-group and taking a weighted sum.
- Could also be done using weighted regression standardization.

# Age-group-specific Pohar Perme estimates

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For each individual  $i$  and time-interval  $j$ :

$d_{ij}$ : all-cause death indicator,

$d_{ij}^*$ : expected deaths based on population life-table estimates.

$y_{ij}$ : individuals time at risk in each interval,  $j$ .

$w_{ij}^{PP} = \frac{1}{S_{ij}^*}$ : a weight to account for differential loss due to other causes based again on population life-tables.

Then, for each age-group,  $k$ , we can calculate the excess mortality rate in each interval  $j$ :

$$\lambda_{jk} = \frac{\sum_{i \in k} w_{ij}^{PP} d_{ij} - \sum_{i \in k} w_{ij}^{PP} d_{ij}^*}{\sum_{i \in k} w_{ij}^{PP} y_{ij}},$$

# Pohar Perme weights ( $w_{ij}^{PP}$ )

Age-standardized survival

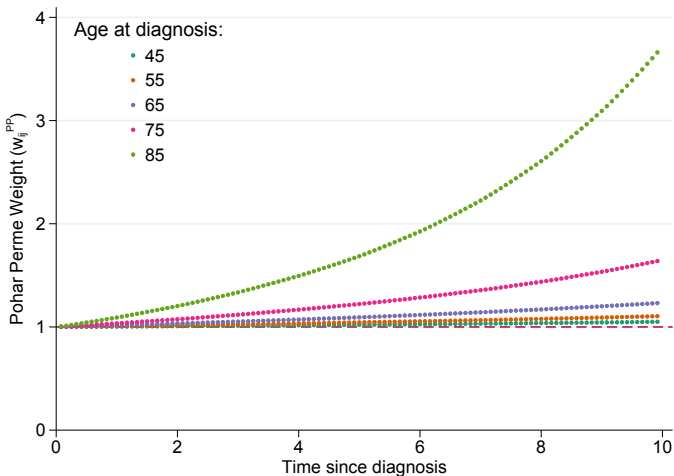
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# Age-group-specific Pohar Perme estimates

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We can convert the excess mortality estimates to the survival scale using the following relationship:

$$R_{jk} = \exp(-\Lambda_{jk}),$$

where the cumulative excess hazard,  $\Lambda_{jk}$  is calculated as

$$\Lambda_{jk} = \sum_j l_j \lambda_{jk}$$

# Externally age-standardised survival

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To convert the age-group specific estimates into an externally standardised estimate using the International Cancer Survival Standard weights:

$$\bar{R}^{ICSS}(t) = \sum_{k=1}^5 w_k^{ICSS} R_k(t),$$

<b>Age-group</b>	<b>w<sub>k</sub><sup>ICSS</sup></b>
15-44	0.07
45-54	0.19
55-64	0.23
65-74	0.29
75+	0.29

# An alternative: the pre-weighting approach

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Could add a further weight,  $w_i^B$ , to re-weight to the external standard and not stratify by age-group:

$$\lambda_j = \frac{\sum_i w_i^B w_{ij}^{PP} d_{ij} - \sum_i w_i^B w_{ij}^{PP} d_{ij}^*}{\sum_i w_i^B w_{ij}^{PP} y_{ij}},$$

where  $w_i^B = \frac{w_i^{ICSS}}{a_i}$ , with  $w_i^{ICSS}$  the value of the external standard weight depending on the age-group of individual,  $i$ , and  $a_i$  is the proportion of people in the age-group to which the individual belongs in the sample.



# Standardization Weights ( $w_i^B$ )

Age-standardized survival

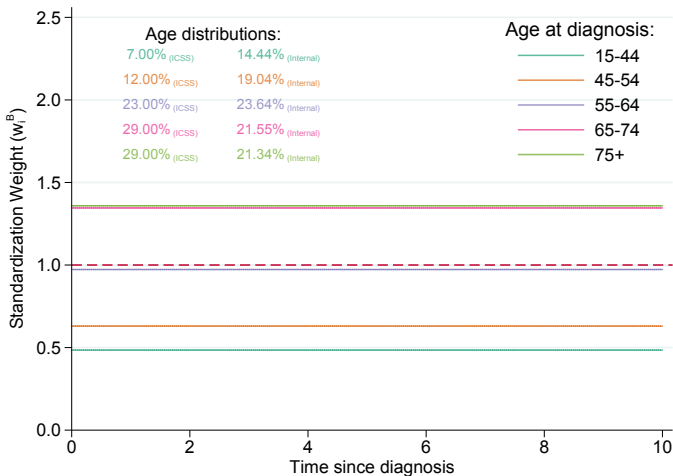
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# Motivating example

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- SEER public-use data for ovarian cancer for 8 US states.
- Restricted calendar years of diagnosis (2005-2009) and the black race group to create sparsity setting.
- Use a state, race, calendar year, age and sex specific lifetable.
- Use the external age ICSS weights for age-standardisation.
- Illustrate the approach with a Pohar Perme approach and a model-based approach (flexible parametric model).

# Ovarian cancer survival: age-group-specific

Age-standardized survival

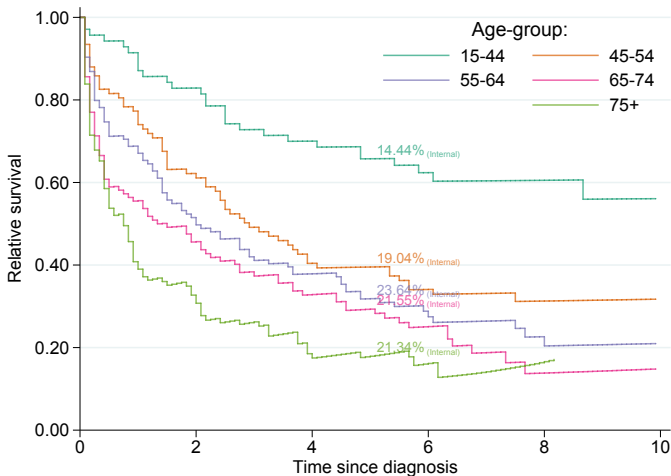
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# Ovarian cancer survival: Internal weights

Age-standardized survival

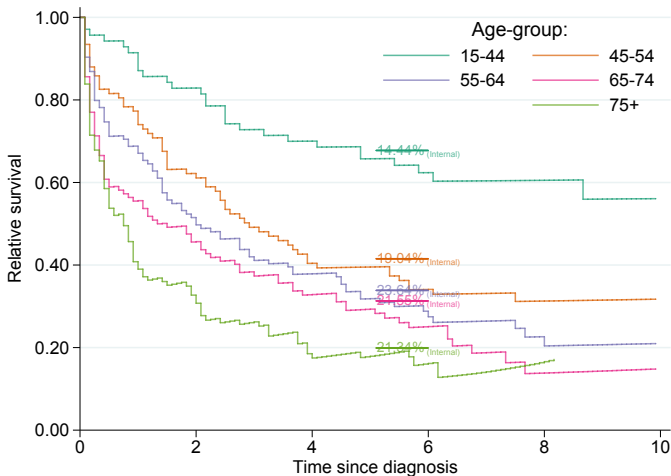
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# Ovarian cancer survival: External weights

Age-standardized survival

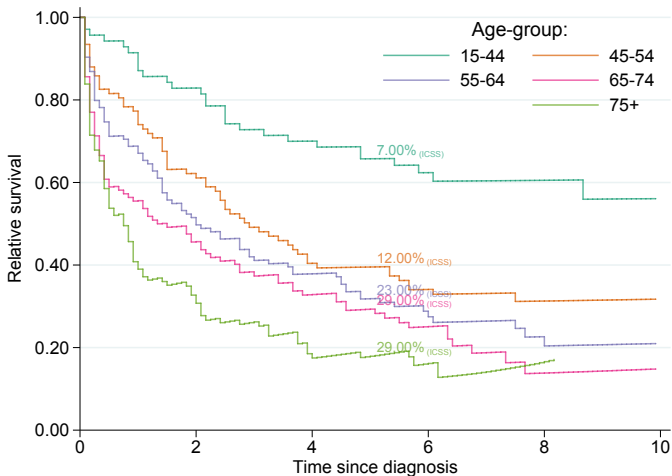
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# Ovarian cancer survival: Traditionally standardised

Age-standardized survival

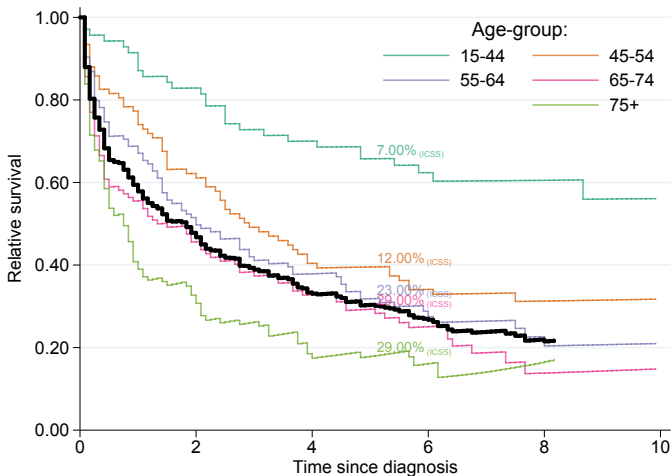
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# Ovarian cancer survival: Pre-weight (all-age)

Age-standardized survival

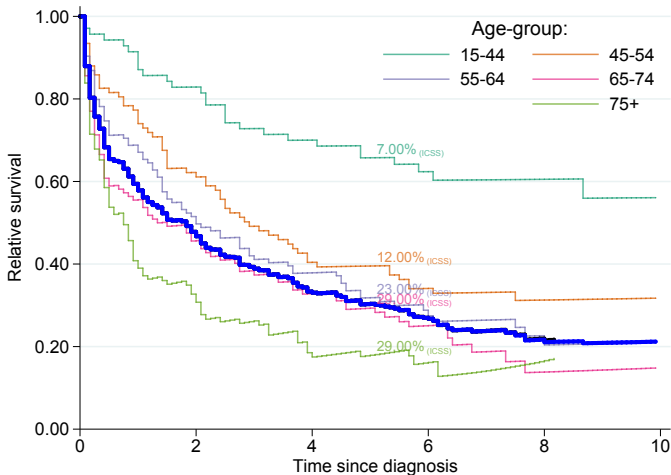
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# Ovarian cancer survival: Internal vs External

Age-standardized survival

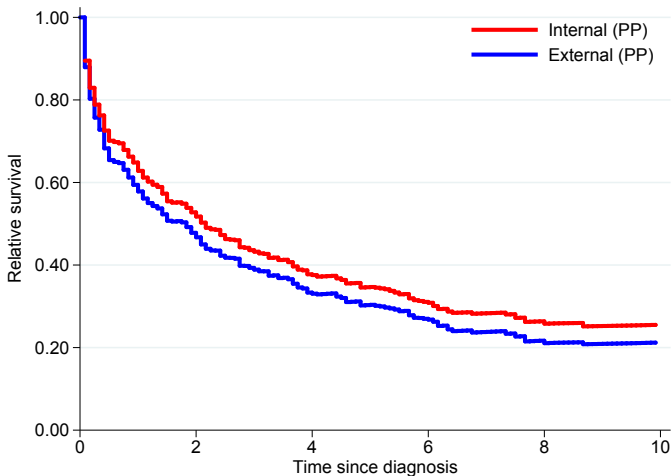
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# Conclusion

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- A Pohar Perme estimate with pre-specified weighting should be used as the non-parametric estimator.
- Parametric models offer an alternative that require careful modelling of covariate and time-dependent covariate effects.
- Care should be taken to correctly specify the internal age distribution in the presence of delayed entry (period analysis estimates).

# Selected References

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